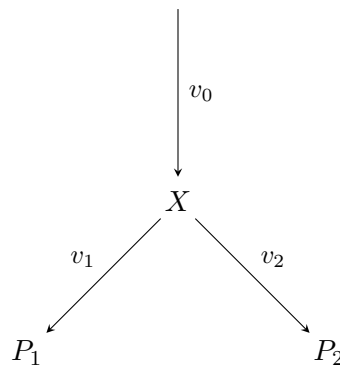


# Exercise Sheet 4

June 29, 2015

## Exercise 1. *Tutorial*

Consider the following network:



The target fluxes are  $v_1$  and  $v_2$ , the corresponding target metabolites are  $P_1$  and  $P_2$  with demand  $\Gamma_1$  resp.  $\Gamma_2$ .

There exist two MGS (Minimal Gene Sets):  $\chi_1 = \{g_0; g_1\}$  and  $\chi_2 = \{g_0; g_2\}$ .

- Which are the corresponding MFM (minimal flux modes)?
- What is the maximal number of different steady-states required to minimize the production time of the demanded output?
- How many possible strategies do we need to consider?
- Sketch the strategies.
- Assume that the kinetic parameters  $\eta$  are set to one:  $\eta_j = 1$  for  $j \in \{1, 2, 3\}$ . Without loss of information we assume further that  $\Gamma_1 = \tau v_1$  and  $\Gamma_2 = \tau v_2$  and set  $r := \frac{\Gamma_1}{\Gamma_2} = \frac{v_1}{v_2}$ . Determine  $\tau$  in dependence to the upper bounds of  $v_j$  and  $\Gamma_i$  for strategy A (only one flux) and B (two fluxes, each produces exactly one product).

- Determine  $\tau$  for strategy A with the values of  $ub$  given by  $ub_0 = 100\text{mol/h}$ ,  $ub_1 = ub_2 = 10\text{mol/h}$  and  $\tau'$  for strategy B with the bounds given by  $ub^1 = ub^2 = \frac{4}{3}ub$ :
  1.  $\Gamma_1 = \Gamma_2 = 50\text{mol}$
  2.  $\Gamma_1 = 90\text{mol}$  and  $\Gamma_2 = 10\text{mol}$

**Exercise 2.** *Homework*

Read the article of Covert, Schilling and Pallson about *Regulation of Gene Expression in Flux Balance Models of Metabolism* (doi:10.1006/jtbi.2001.2405), with special focus on a specific example:

1. EXAMPLE 1 – DIAUXIE ON TWO CARBON SOURCES  
Marthe & Balduin
2. EXAMPLE 2 – AEROBIC/ANAEROBIC DIAUXIE  
Marjan & Moritz
3. EXAMPLE 3 – GROWTH ON CARBON AND AMONI ACID WITH CARBON IN EXCESS  
David & Pascal