



GSNAP: Fast and SNP-tolerant detection of complex variants and splicing in short reads

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Introduction

Motivation

GSNAP Features

Examples of Complex Variant Detection

Outline

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- Summary

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- Method 1: Spanning Set Generation and Filtering

- Method 2: Complete Set Generation and Filtering

- Verification of Candidate Regions

- Detecting Insertions and Deletions

- Detecting Splice Junctions

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- Simulated Reads
- Transcriptional Reads
- Limitations

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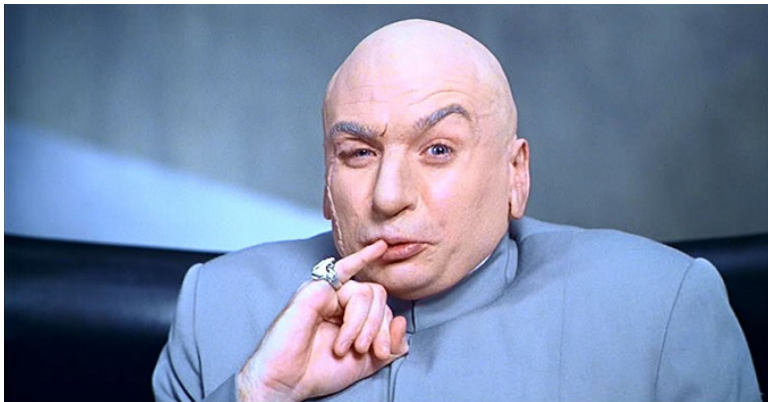
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- ▶ "Why should we be happy with millions of reads, when we can have...



...billions?"

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- ▶ Current (Feb 2010) read mappers tend to either be very fast (BWA, Bowtie, SOAP2) or sensitive to variants (SOAP)
- ▶ GSNAP is intended to be fast and able to handle complex variants

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- ▶ Still pretty fast

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Long deletion of 17nt plus mismatches

- ▶ 17nt deletion matching an entry in dbSNP, including mismatches:

C1QC (NM_172369), 3' UTR, chr +1

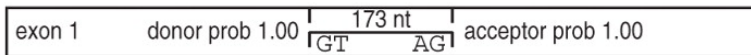
TCCTTGCCTAGACCATTCTCCCCACCAGATGGACTTCTCCTCCAGGGAGCCCACCCTGAC
 rs60255495

```

TCCTgGCCTAGACCATTCTCC-----CCTCCAGGGAGC
CCTTGCCgAGACCATTCTCC-----CCTCCAGGGAGCC
  TTGCCTAGACCATTCTCC-----CCTCCAGGGAGCagA
    CTAGACCATTCTCC-----CCTCCAGGGAGCCCACCCT
      tACCATTCTCC-----CCTCCAGGGAGCCCACCCTGAC
    
```

- ▶ An intron within exon 1 of HOXA9. Is also experimentally supported.

HOXA9 (NM_152739), chr -7

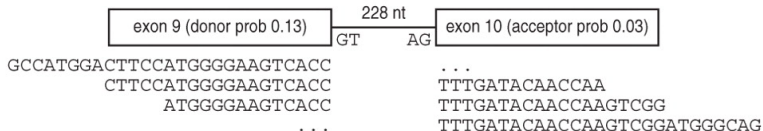


GGCGGCGCCGGACGGCAG
CGGCGCCGGACGGCAG

TTGATAGAGAAAAAC
TTGATAGAGAAAACAA

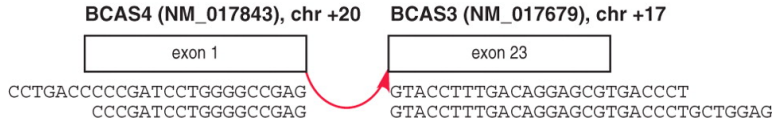
- ▶ Splicing sites identified despite having low probabilistic scores.

TSTA3 (NM_003313), chr -8

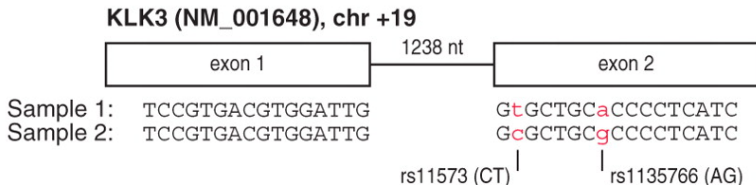


Interchromosomal splicing (gene fusion)

- ▶ Splicing between BCAS4 (chr 20) and BCAS3 (chr 17).



- ▶ SNP-tolerance allows both genotypes to align well



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- ▶ Verify the number of mismatches by checking the whole read against the reference

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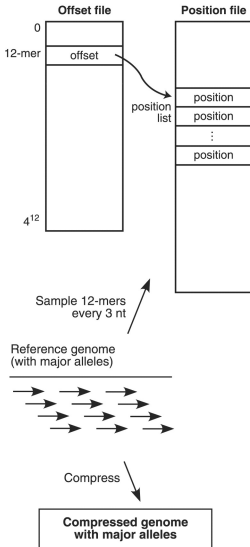
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- ▶ Entire table only needs to be in memory during construction. Afterwards it is mmap'd and only part is loaded into memory.

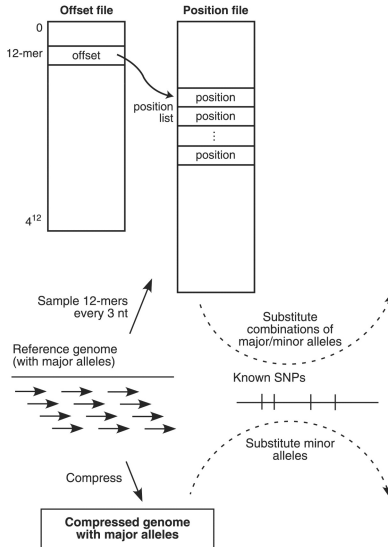
Hashing the Reference Genome

A Hash table indexing of a reference sequence

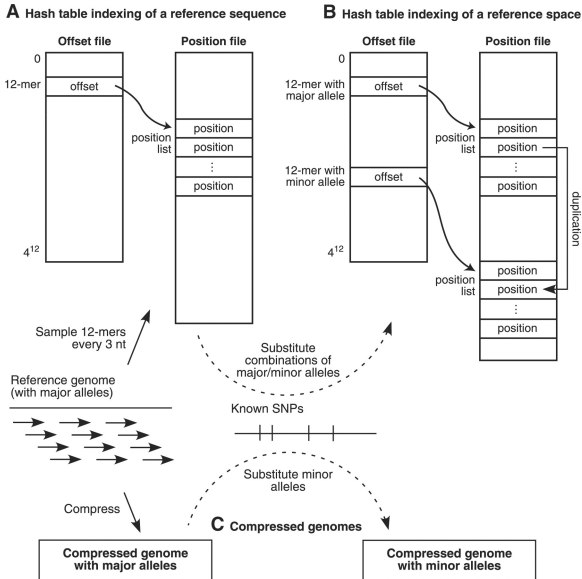


Including SNPs

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Resulting Reference "Space"



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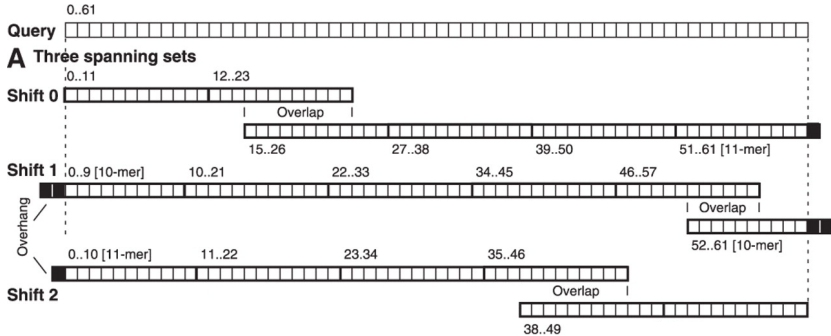
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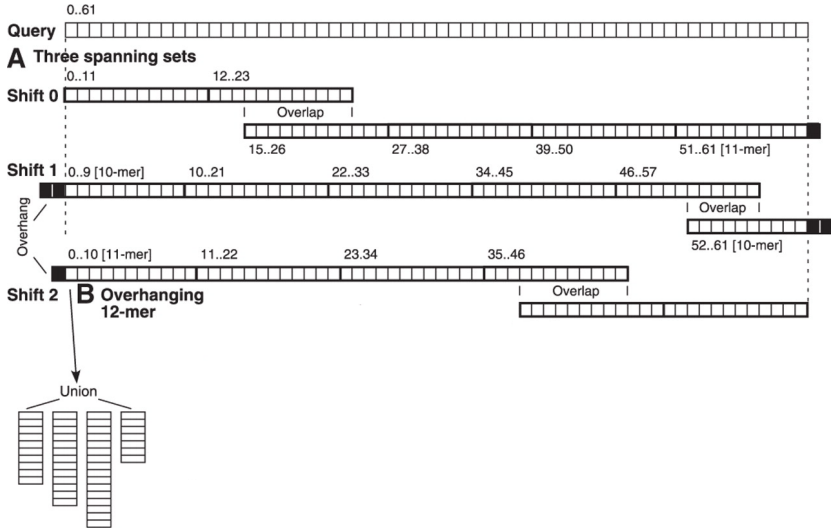
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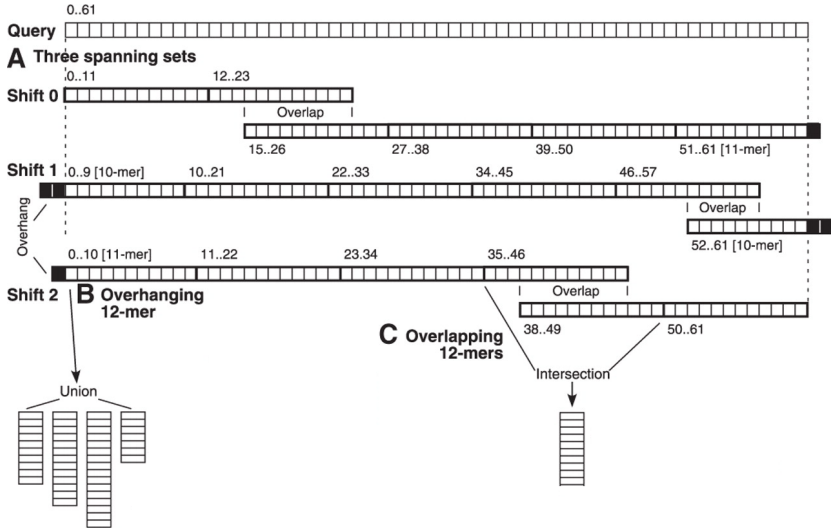
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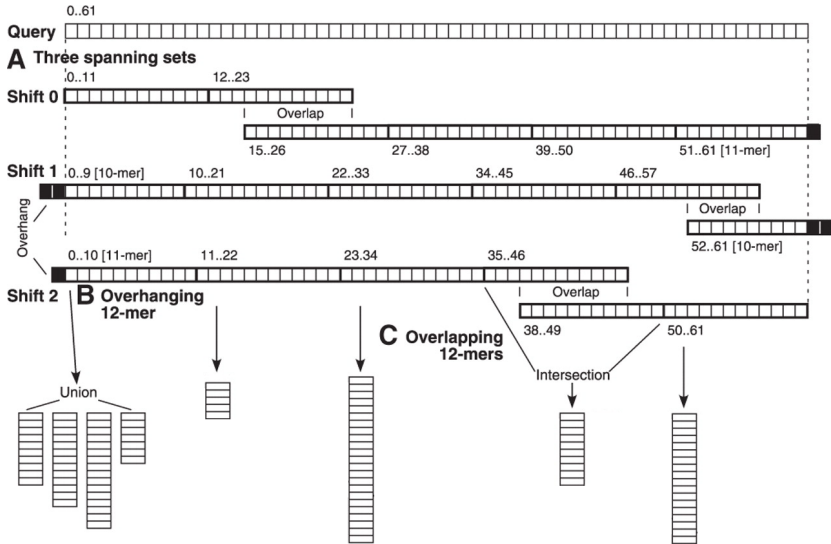
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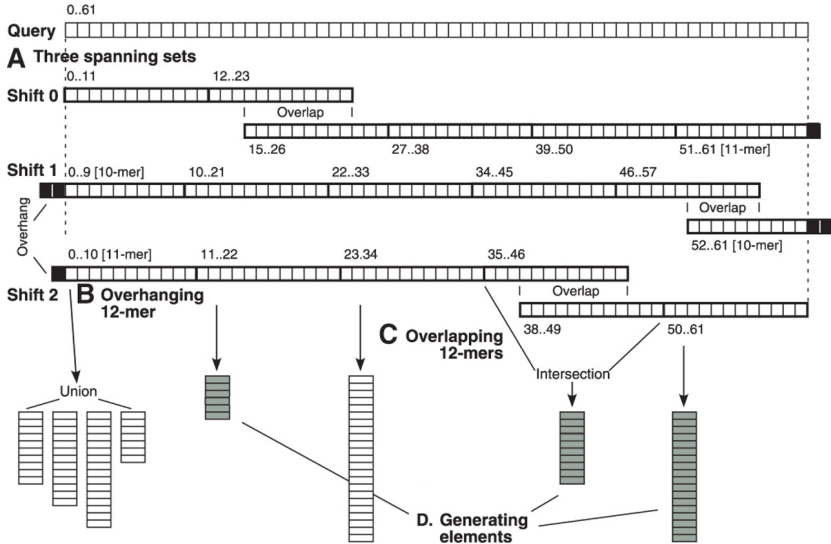
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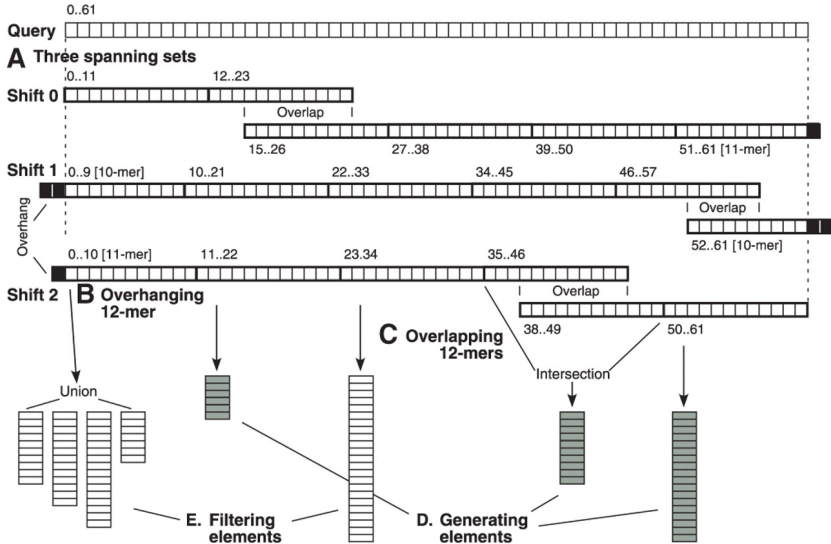
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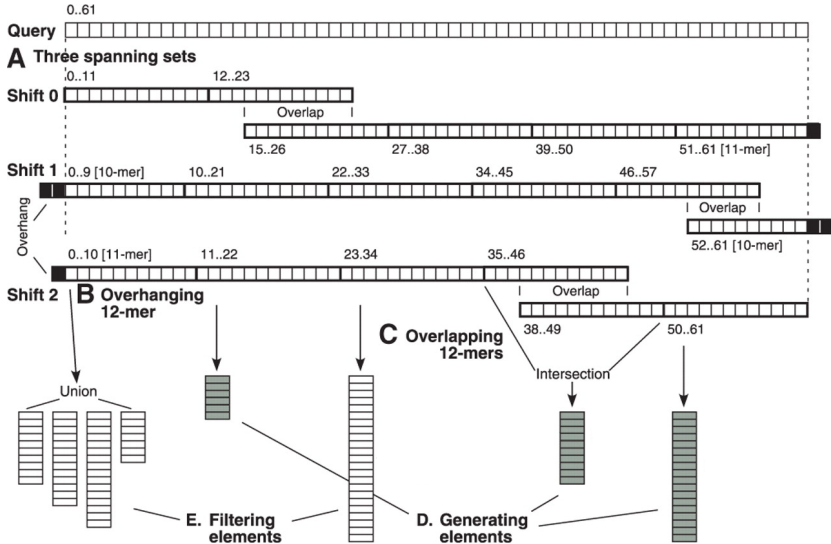
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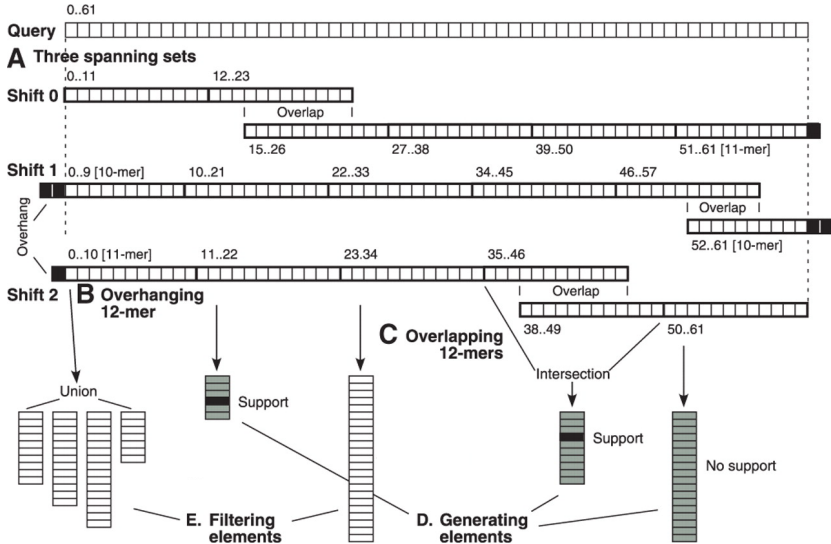
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- ▶ They choose $K + 2$ generating sets, where K is the constraint score (= max number of mismatches)

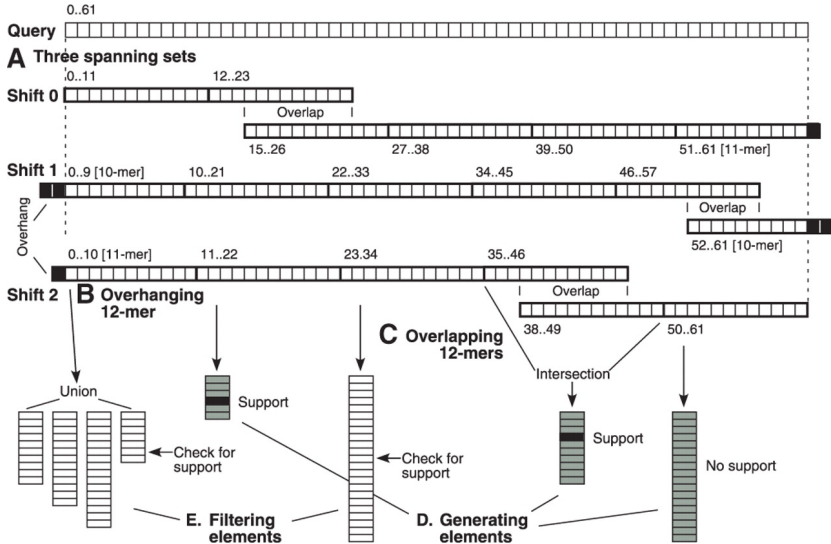
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- ▶ For reads of length 400 (454), the we can allow a maximum of 31 mismatches.

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- ▶ If we want to allow larger numbers of mismatches or the same number of mismatches in shorter reads, we need to use another method...

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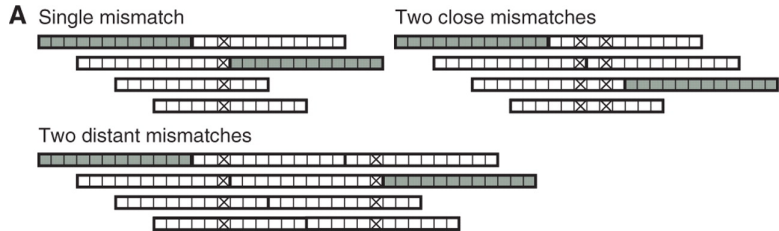
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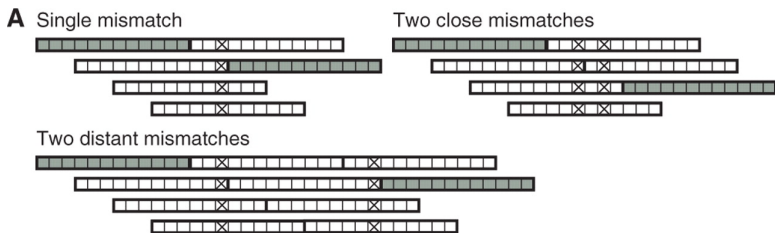
- Simulated Reads
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Conclusions

- ▶ Uses the complete set of overlapping 12mers.
- ▶ Works for any number of mismatches as long as read and target have ≥ 14 consecutive matches (12mer out of phase by up to two bases)
- ▶ Exhaustive for $K \leq \lfloor L/14 \rfloor - 1$

Complete set generation and filtering





- ▶ Lower bound on mismatches: $\lfloor (\Delta p + 6)/12 \rfloor$
 where Δp is the distance between start locations of consecutive supporting 12mers.

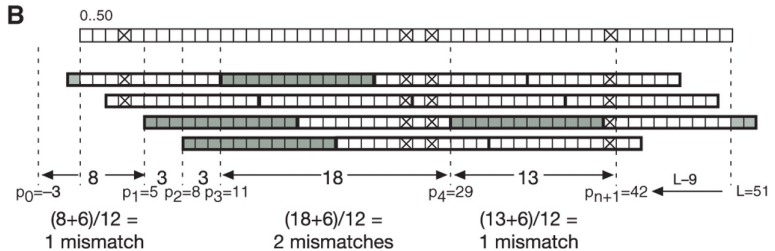
Complete set example

B

0..50



Complete set generation and filtering



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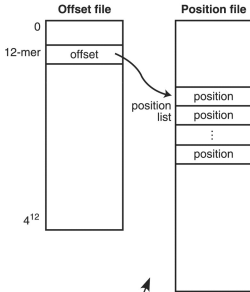
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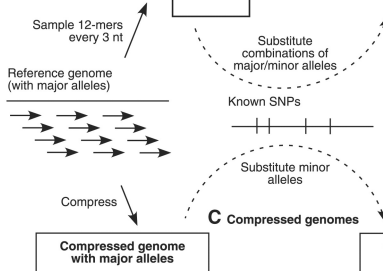
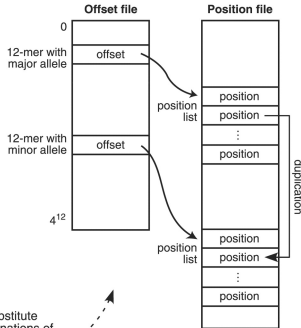
- ▶ The spanning set and complete set methods generate candidate regions for which we know a **lower bound** on the number of mismatches.
- ▶ These regions need to be verified to check the **exact number** of mismatches.

Remember: Resulting Reference "Space"

A Hash table indexing of a reference sequence



B Hash table indexing of a reference space



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- ▶ Because we have a reduced alphabet the reference is stored as 3 bits per character: 2 bits for the nt + a flag
 - ▶ Flag in major-allele genome: indicates unknown or ambiguous nt
 - ▶ Flag in minor-allele genome: indicates a SNP

- ▶ Query sequence converted to the same compressed representation as the reference
- ▶ Shifted into position and bitwise XOR combined with the major- and minor-allele genomes separately
- ▶ Resulting arrays are bitwise AND'd, so mismatches at a SNP only occur if both alleles do not match

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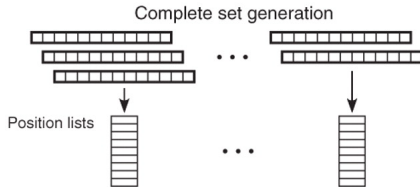
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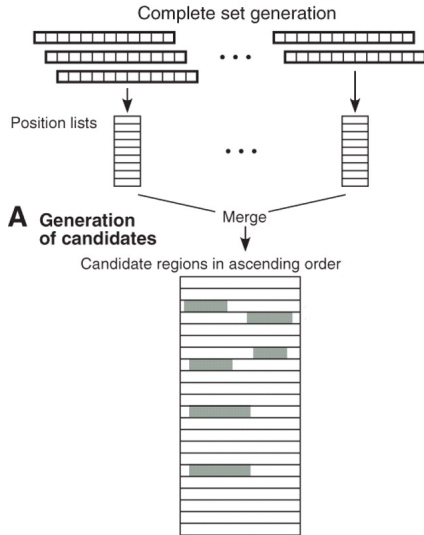
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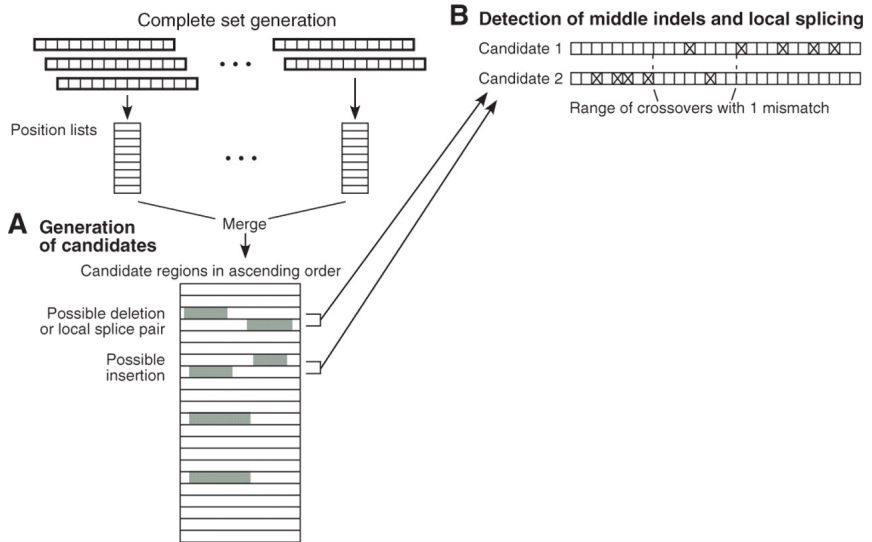
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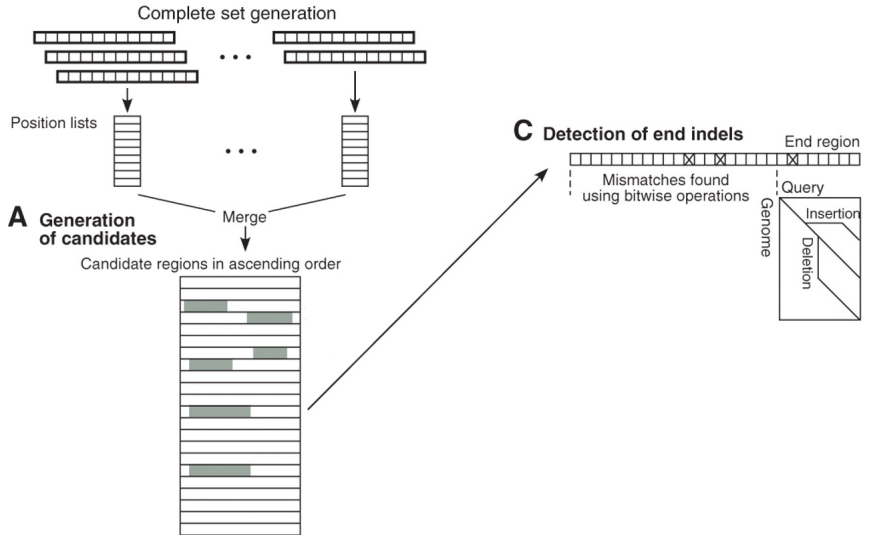
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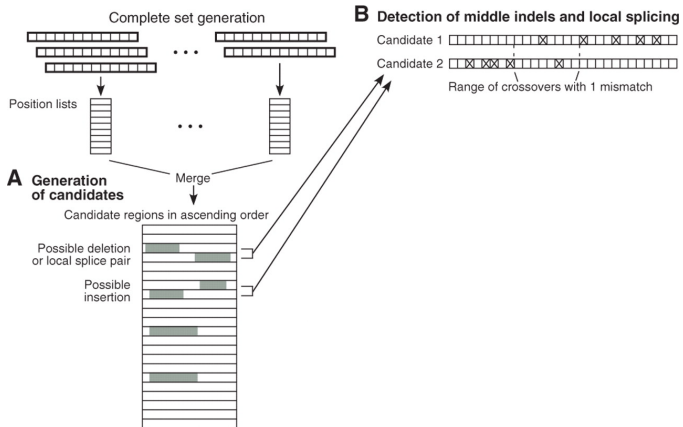
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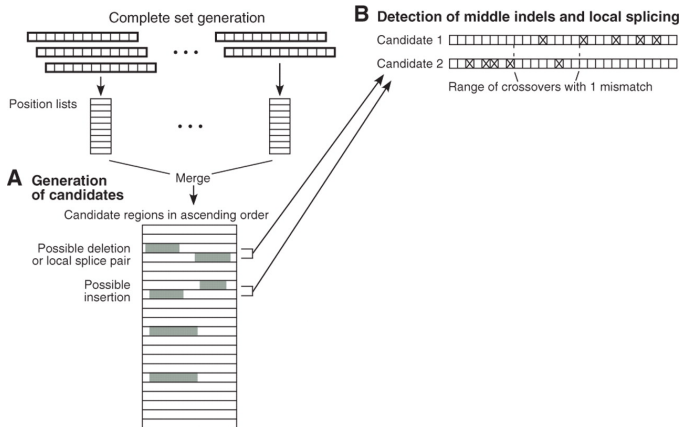
- ▶ Known splice sites: user-provided database
- ▶ Novel splice sites: maximum entropy probabilistic model from Yeo and Burge, 2004

- ▶ Short-distance splice sites are on the same chromosome and < some distance apart (default: 200,000 nt)
- ▶ Method similar to the one we used to find middle deletions earlier. . .

Detecting Splice Junctions



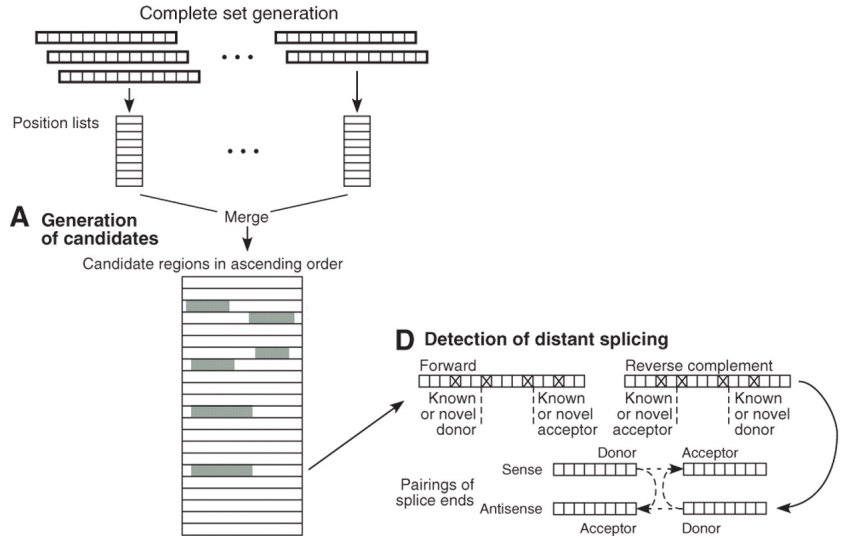
Detecting Splice Junctions



- ▶ Crossover area is then searched for donor or acceptor sites (either known or novel with high probability).

- ▶ Long-distance splice sites can be on different chromosomes
- ▶ Require higher probability scores for novel splice sites than short-distance splice sites
- ▶ Candidates with matching breakpoints on the read are matched

Detecting Splice Junctions



- ▶ If both splice sites can not be found then GSNAP will return one site (a "half-intron")

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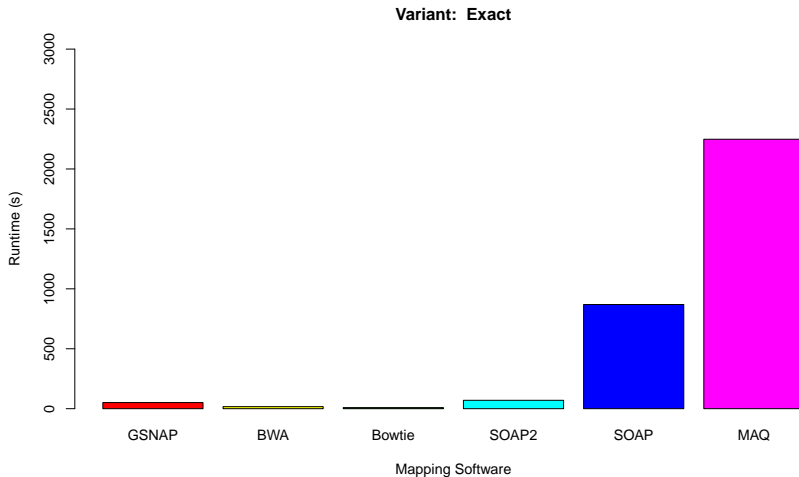
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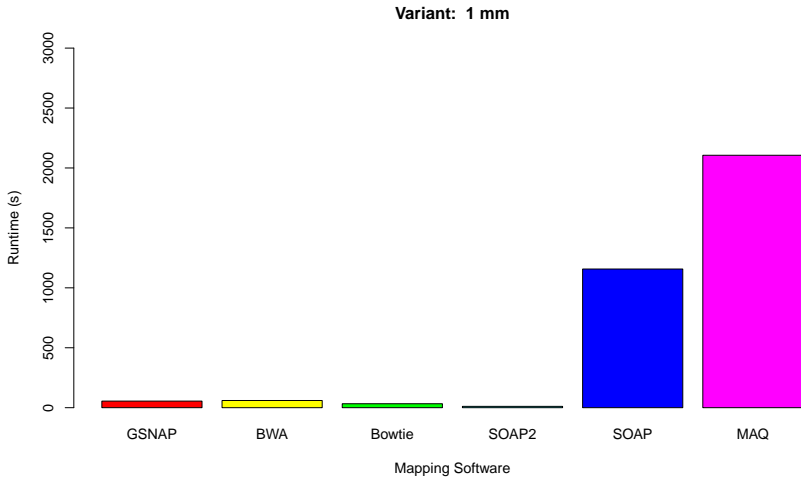
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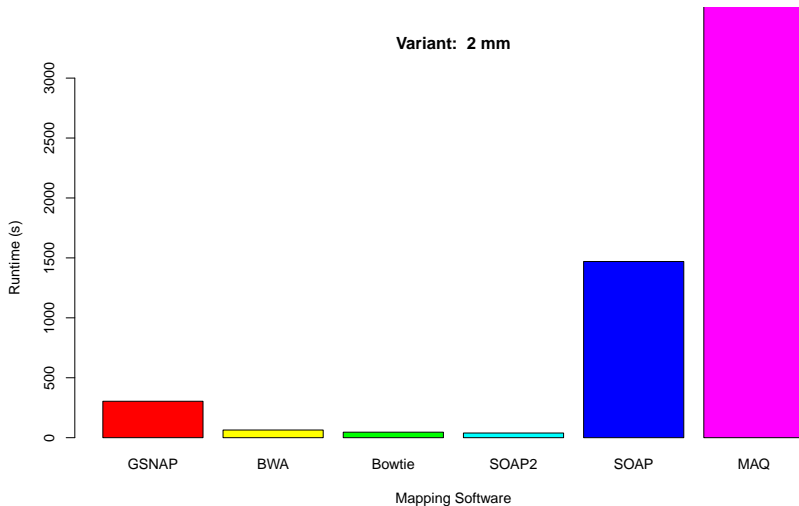
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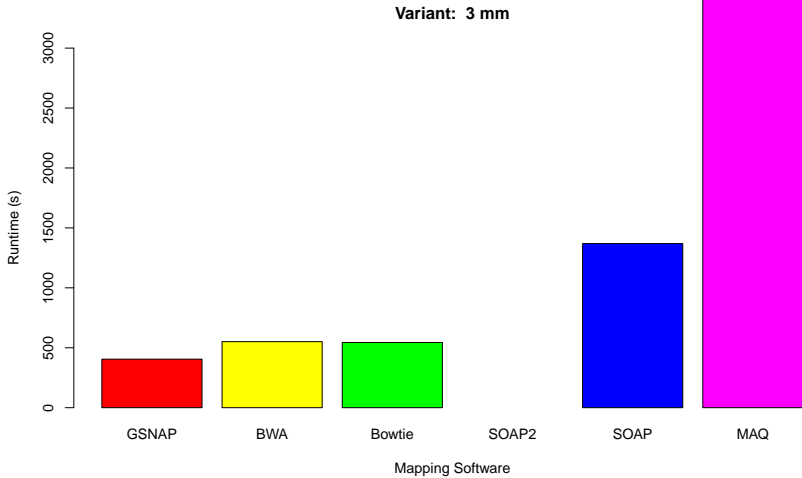
Conclusions

- ▶ Runtime comparison between GSNAP and other alignment tools (for 100,000 reads)
- ▶ Simulated increasingly complicated variants
 - ▶ exact matches only
 - ▶ 1 - 3 mismatches
 - ▶ short insertions and deletions
 - ▶ longer insertions and deletions

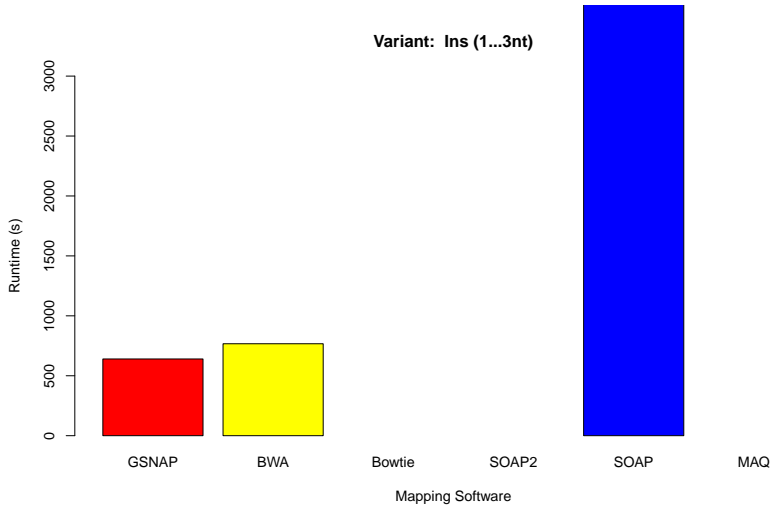


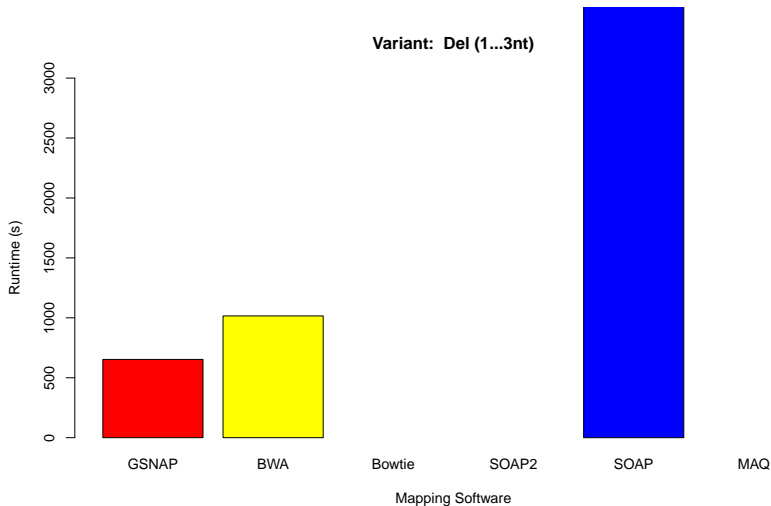


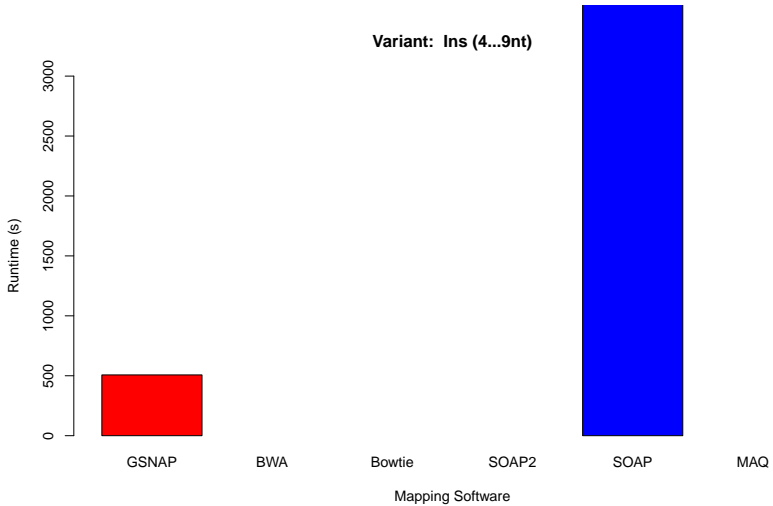




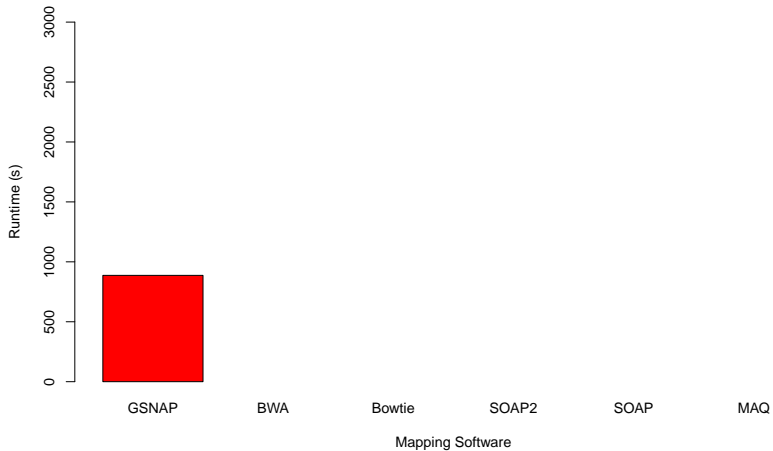
Simulated Reads: 36nt



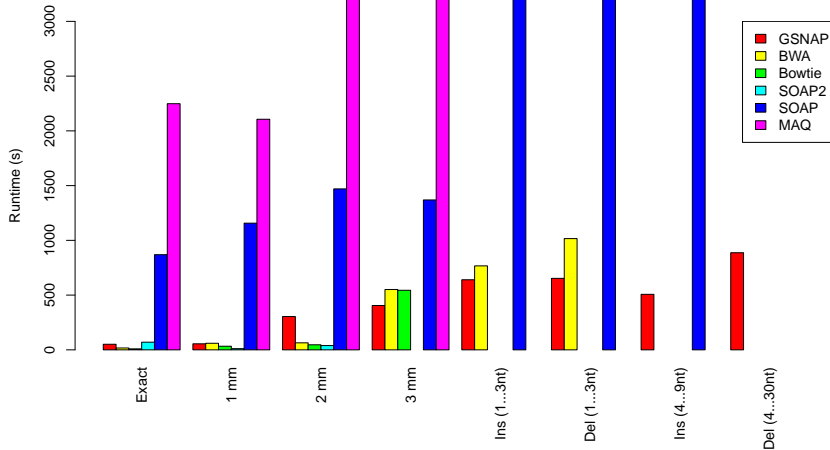




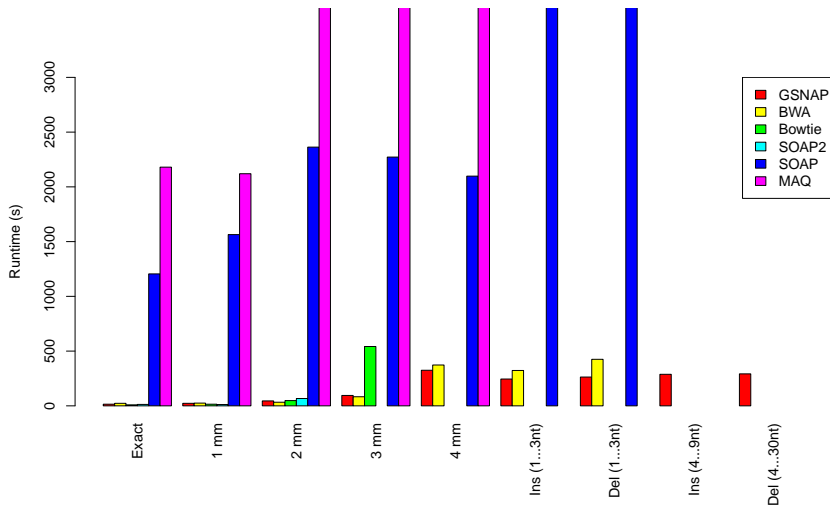
Variant: Del (4...30nt)



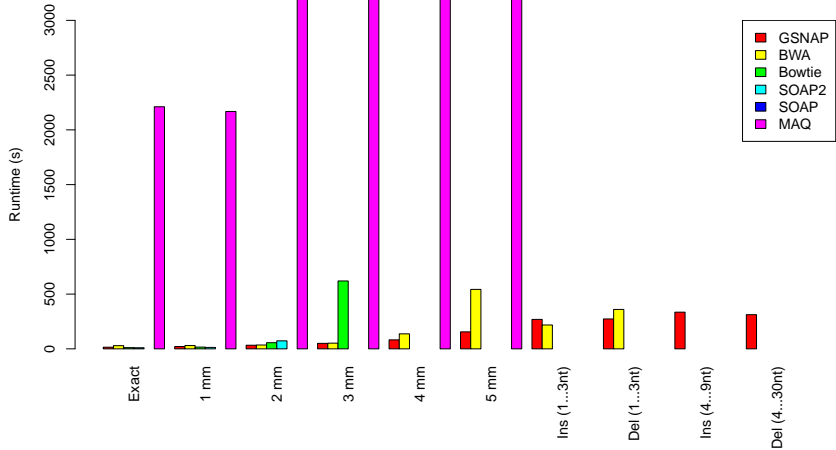
Simulated Reads: 36nt



Simulated Reads: 70nt



Simulated Reads: 100nt



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- ▶ SOAP: 15% misses for 36nt reads with 3 mismatches, around 5% for 1-3nt indels
- ▶ BWA: 1-5% misses in 1-3nt indels

Memory Requirements

- ▶ GSNAP: should have access to 5 GB of memory, otherwise it will run slowly
- ▶ BWA: 2.2 GB
- ▶ Bowtie: 1.1 GB (exact matches) or 2.2 GB (allowing mismatches)
- ▶ MAQ: 302 MB
- ▶ SOAP: 14 GB
- ▶ SOAP2: unknown ("only provided as a binary and did not have the required compile time flag")

Outline

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- GSNAP Features
- Examples of Complex Variant Detection

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- Method 2: Complete Set Generation and Filtering
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- ▶ Including known splicing information → increased yield approx. 8%
- ▶ Including SNP tolerance → minor increase in yield (0.5%) but effected about 8% of alignments

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- ▶ Limited to one indel or splice site per read
- ▶ Does not use read quality scores
- ▶ Does not work with ABI SOLiD data

- ▶ Comparable to other fast read alignment algorithms in terms of speed, but can handle more complex variants and splicing

For Further Reading I

-  **Knuth D.E.**
The Art of Computer Programming: Sorting and Searching. Vol 3.
Addison-Wesley, 1973
-  **Thomas D. Wu and Serban Nacu**
Fast and SNP-tolerant detection of complex variants and splicing in short reads
Bioinformatics, 2010 Apr 1;26(7):873-81.
-  **Yeo G and Burge CB.**
Maximum entropy modeling of short sequence motifs with applications to RNA splicing signals
J Comput Biol. 2004;11(2-3):377-94.

- ▶ Optional

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