

Algorithms

WS 2013/14

Exercises 7

1. Turing machine simulation (NIVEAU I)

Given a Turing machine M accepting the language $L = \{0^n 1^n \mid n \geq 1\}$ with accepting state q_4 and the next move function δ :

| δ | 0 | 1 | X | Y | # |
|----------|---------------|---------------|---------------|---------------|----------------|
| q_0 | (q_1, X, R) | — | — | (q_3, Y, R) | — |
| q_1 | $(q_1, 0, R)$ | (q_2, Y, L) | — | (q_1, Y, R) | — |
| q_2 | $(q_2, 0, L)$ | — | (q_0, X, R) | (q_2, Y, L) | — |
| q_3 | — | — | — | (q_3, Y, R) | $(q_4, \#, R)$ |
| q_4 | — | — | — | — | — |

- Simulate M on input 0011 and 001101.

2. Decision problems (NIVEAU II)

Let w_i be the i -th word in $\{0, 1\}^*$ and M_n the n -th turing machine. Consider:

- the general halting problem K : “Does Turing machine M_n halt for input w_i ?”
and
- the special halting problem K' “Does Turing machine M_n halt for input w_n ?”

- Prove that K' is undecidable but semi-decidable.
- Use reduction to prove that K is undecidable.