WHAT IS THE GEOMETRIC MEANING OF THE VIRTUAL COHOMOLOGICAL DIMENSION OF A GROUP?

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ABSTRACT. In this talk we present a triangulated category of proper G-spectra where G is an infinite discrete group with bounded torsion and with finite dimensional $\underline{E}G$. The triangulated category is generated by the orbits with finite isotropy and admits restriction functors to genuine H-spectra for any finite subgroup H of G. We also indicate how a proper G-spectrum gives rise to a Mackey functor for G. This is joint work with Degrijse, Lück and Schwede. We will also discuss a second project, joint with Bárcenas and Degrijse, where we apply this setup to define a notion of stable geometric dimension for proper actions of G. We prove that this notion of dimension coincides with the Mackey cohomological dimension of G. If G is virtually torsion free, the Mackey cohomological dimension is known to equal the virtual cohomological dimension of G. Hence we obtain a geometric interpretation of the virtual cohomological dimension of G.