

FREIE UNIVERSITÄT BERLIN  
Fachbereich Mathematik und Informatik

Promotionsbüro, Arnimallee 14, 14195 Berlin

## DISPUTATION

**Donnerstag, 22. Januar 2015, 11.00 Uhr**

**Ort: Seminarraum, ZIB, Takustr. 7, 14195 Berlin**

**Disputation über die Doktorarbeit von**

**Herrn Dennis Clemens**

**Thema der Dissertation:  
Two-player games on graphs**

**Thema der Disputation:  
Reiher's Clique Density Theorem**

Die Arbeit wurde unter der Betreuung von **Prof. T. Szabó, PhD** durchgeführt.

**Abstract:** One of the most classic results in Extremal Graph Theory is Turán's Theorem, which guarantees the existence of cliques of given order  $r$  in a graph  $G$ , provided that its edge density  $d$  exceeds a certain threshold. Naturally, one may wonder how many such cliques must necessarily be contained in  $G$  when the edge density  $d$  becomes larger than this threshold. Lovász and Simonovits [1] conjectured their number to be at least  $F_r(d)n^r + O(n^{r-2})$ , where  $F_r$  describes a certain piecewise concave function. After some partial results in the last decades, the conjecture was proven by Christian Reiher [2] recently, by using weighted graphs and Lagrange multipliers which help to transfer this discrete problem into a continuous setting. In the talk we will see a construction showing that the above bound is tight asymptotically and then we will see an overview on the proof by Christian Reiher.

[1] L. Lovász and M. Simonovits: On the number of complete subgraphs in a graph II, Studies in pure mathematics, pages 459-495, Birkhäuser, 1983.

[2] C. Reiher: The Clique Density Theorem, Hamburger Beiträge zur Mathematik 462, pages 1-25, 2012.

Die Disputation besteht aus dem o. g. Vortrag, danach der Vorstellung der Dissertation einschließlich jeweils anschließenden Aussprachen.

**Interessierte werden hiermit herzlich eingeladen**

Der Vorsitzende der Promotionskommission  
Prof. T. Szabó, PhD