

# Sequence Analysis SS 2013

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Sommersemester 2013

9. Exercise sheet, July 5th, 2013  
Discussion: July 10th, 2013

*Exercise 1.*

Minimal Resolved Match Refinement

Prove the following Lemma:

**Lemma 1.** *There exists a unique resolved refinement  $\bar{S}$  of  $S$  of minimal cardinality.*

**Proof:** Sketch: Consider two different resolved refinements  $\mathcal{S}_1$  and  $\mathcal{S}_2$  of  $\mathcal{S}$ , both of minimal cardinality. Divide proof into two cases. 1)  $(supp_A(\mathcal{S}_1) \neq supp_A(\mathcal{S}_2))$  2)  $(supp_A(\mathcal{S}_1) = supp_A(\mathcal{S}_2), supp_B(\mathcal{S}_1) = supp_B(\mathcal{S}_2))$

*Exercise 2.*

Match Refinement Example

Given Sequences  $A=AAGCGCCCGCG$  and  $B=AAGCGGGCCCGCG$  and the projection maps:

$$\begin{array}{ll} \alpha_{S_1}[0, 5] \rightarrow [0, 5] & \beta_{S_1}[0, 5] \rightarrow [0, 5] \\ \alpha_{S_2}[2, 5] \rightarrow [11, 14] & \beta_{S_2}[11, 14] \rightarrow [2, 5] \\ \alpha_{S_3}[8, 11] \rightarrow [2, 5] & \beta_{S_3}[2, 5] \rightarrow [8, 11] \\ \alpha_{S_4}[5, 11] \rightarrow [8, 14] & \beta_{S_4}[8, 14] \rightarrow [5, 11] \end{array}$$

- Draw the two sequences and their corresponding segment matches.
- Compute the minimal resolved refinement by applying the algorithm from the lecture.